# JES ISS EXAM, 2010

Serial No.

1801

C-HLR-K-TD

## STATISTICS—IV

Time Allowed: Three Hours

Maximum Marks .

200

#### INSTRUCTIONS

Candidates should attempt FIVE questions in all including Question nos. I and 5 which are compusors and attempt remaining THREF questions by choosing at least ONE each from Sections A and B.

The number of marks carried by each question is indicated at the end of the question.

Answers mys. be written in ENGLISH.

Symbols and abbreviations are as usual.

If the data is required to be assumed for an vering a question, it may be suitably ssumed, indicating this clearly.

### SECTION-A

- 1. Attempt any FIVE parts :-
  - (a) Give a brief critical account of Poisson process.

- Let  $\phi$  designate the set of all feasible solution to the linear program in standard form. Then prove that every extreme point of  $\varphi$  has at least n-m zero components and is a basic feasible solution.
- Obtain differential-difference equations for a fin (c) death process.
- (d) Describe Vogel's method transportation problem.
- Explain how the theory of replacement is used (e) in:
  - replacement of item. (i) those maintenance cost varies with time
  - replacement of tems that fail completely. (ii)
- (f) Explain the te
  - (i) ion of queues

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- ge inventory level
- Group replacement.

w that in a simple Random walk with two eflecting barriers at 'o' and 'a', the stationary distribution  $\pi_{i}$  is given by :

$$\pi_j = \frac{1 - p/q}{1 - (p/q)^{a+1}} (p/q)^j, j = 0, 1, ..., a$$

where  $\pi_j = \lim_{n \to \infty} p_{ij}^{(n)}$ ; and  $p_{ij}^{(n)}$  has the usual

(Contd.)

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interpretation that it represents the probability that the particle occupies the state j at time n having started in the state i; what will be the value of  $\pi_i$  when the Random walk is homogeneous (i.e., p = q)?

- Investigate the M | M | 1 queueing mode by (b) Markov chain technique.
- Let {X<sub>t</sub>} be a stochastic process of independent increments. If  $P(X_{t_0} = \alpha) = 1$  for some epoch  $t_0$ and some constants  $\alpha$ , then show that  $\{X_i\}$  is a Markov process.
- $\mathbf{h}^{\text{th}}$  generation, n = 0, 1,(d) Let X<sub>n</sub> denote the size 2, ....., and  $X_0$ . Then the r.v.  $y_n = \sum_{i=1}^{n} X_i$ , denotes the total number of progeny. Then, show that the f.f. R<sub>n</sub>(s) of Y<sub>n</sub> satisfy the recurrence

$$R_{n}(s) = sP(R_{n-1}(s)),$$

relation:

there P(s) being the p.g.f. of the offspring 10 distribution.

If either the primal or the dual problem has a finite optimum solution, then show that the other problem 10 has a finite optimum solution.

- (b) Define a transportation problem. Obtain the necessary and sufficient condition for the existence of a feasible solution to a transportation problem.
- For a given homogeneous M | M | K qu (c) system, if the steady state probabilities xis prove that the traffic intensity of the system is less than unity. 10
- Solve the following LP problem (d) Simplex method:

Minimize:

$$Z = 80x_1 + 60$$

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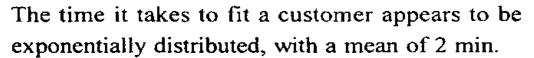
subject to:

$$0.20x_{1} - 0.25x_{2} \le 0.25$$

with x non-negative.

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pen's department of a large store employs one or for customer fittings. The number of istomers requiring fittings appears to follow a Poisson distribution with mean arrival rate 24 per hour. Customers are fitted on a first-come, firstserved basis, and they are always willing to wait for the tailor's service, because alterations are free.



- (i) What is the average number of customers in the fitting room?
- (ii) How much time should a customer expect to spend in the fitting room?
- (iii) What percentage of the time is the tail and the
- (b) If  $X_n = \max \{Y_1, Y_2, \dots, Y_n\}$ , where  $Y_i$  denotes the number on the face turning  $x_i$  is a Markov chain. Obtaining transition matrix.

(c) A large number of special light bulbs are used in a precision assembly thop all of which must be kept in working order. If a bulb fails in service it costs Rs. 20 to replace it. If we replace all the bulbs in the same operation, we can do it only for Rs. 7 a bulb. The probability distribution of lives are at follows:

Failure week		1	2	3	4	5	6
Probability	:	0.09	0.16	0.24	0.36	0.12	0.03

Calculate the week of group replacement so that the average cost is minimum.

(d) Describe the ABC inventory classification system.

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		SECTION—B
5.	Att	empt any FIVE parts :
	(a)	and structure of a complete life table.
		Explain how the different columns of a life table
		may be computed on the basis of observed age-
		specific mortality rates.
	(b)	or it and rish it, and indicate why
		each is considered an improvement on the
		preceding measure of fertility 4
	(c)	Derive Makeham's formula, starting from suitable
		assumptions.
	(d)	What do you mean by intensic growth rate? Derive
		an expression for in rinsic growth rate from Lotka's
		renewal equation.
	(e)	(i) Find the binary equivalent of (23) <sub>10</sub> .
		(ii) Pin the hexadecimal equivalent of (41819) <sub>10</sub> .
		(iii) Ping the decimal equivalent of the
		desimal equivalent of the
	ക്ര	hexadecimal number $(0.4c)_{16}$ .
	1	Sescribe different types of databases. 8
	(0)	Discuss the relative importance of logistic and

component methods of population projections.

(b) Describe the different methods of computing the infant mortality rate. 10

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(c) The following table relates to the all India female population (1951), the number of female live births classified according to the age of mothers and the survival rate for females. Calculate the GRR and NRR.

Age	Female Population	Total number of female live births	Survival at (per 100,000)	
	(100)	(100)		
1519	157670	4632	8065	
20-24	147624	14443	55870	
25—29	124200	14058	52981	
30—34	105865	8210	48963	
35—39	89264	4636	44146	
4044	77887	2158	39154	
45—49	61161	689	34198	

(d) Explain the following:—

(i) ge pyramid

Standardization of vital rates

(iii) Migration models.

10

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7. (a) Discuss migration analysis based on place of birth data. What are the drawbacks of this method?

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(Contd.)

	(b)	What is age bearing 2 Hames	
	(4)	Be troping : How can you deter	
		presence in census age data? Explain Wip index.	ple's
			10
	(c)	purpose of memory in a compa	ter?
		What are the main characteristics of a ma	mory
		cell?	10
	(d)	Explain the following:	
		(i) Data entry database	
		(ii) Data manipulation language	
		(iii) On-line real time processing.	10
8.	(a)	What criteria are used in selecting a comp	outer
		network topology	10
	(b)	Outline the ses of SQL (Structured Qu	uerv
		Language) to the data administration.	10
	(c)	Describe the lature and properties of stable	
.•		statical ry populations.	10
	(d)	Define Gompertz curve and explain a met	-
		of fixing the curve to a given and Co.	
		igures.	
	N		10
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